



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

Impact of spatial averaging on radar reflectivity at internal snowpack layer boundaries

Citation for published version:

Rutter, N, Marshall, H, Tape, K, Essery, R & King, J 2016, 'Impact of spatial averaging on radar reflectivity at internal snowpack layer boundaries', *The Journal of Glaciology*, pp. 1-10.
<https://doi.org/10.1017/jog.2016.99>

Digital Object Identifier (DOI):

[10.1017/jog.2016.99](https://doi.org/10.1017/jog.2016.99)

Link:

[Link to publication record in Edinburgh Research Explorer](#)

Document Version:

Publisher's PDF, also known as Version of record

Published In:

The Journal of Glaciology

Publisher Rights Statement:

COPYRIGHT: © The Author(s) 2016

This is an Open Access article, distributed under the terms of the Creative Commons Attribution licence (<http://creativecommons.org/licenses/by/4.0/>), which permits unrestricted re-use, distribution, and reproduction in any medium, provided the original work is properly cited.

General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



Impact of spatial averaging on radar reflectivity at internal snowpack layer boundaries

N. RUTTER,¹ H.-P. MARSHALL,² K. TAPE,³ R. ESSERY,⁴ J. KING⁵

¹Department of Geography, Northumbria University, Newcastle upon Tyne, UK

²Center for Geophysical Investigation of the Shallow Subsurface, Boise State University, Boise, ID, USA

³Institute of Northern Engineering, Water & Environmental Research Center, University of Alaska, Fairbanks, AK, USA

⁴School of GeoSciences, University of Edinburgh, Edinburgh, UK

⁵Climate Research Division, Environment and Climate Change Canada, Toronto, Canada

Correspondence: N. Rutter <nick.rutter@northumbria.ac.uk>

ABSTRACT. Microwave radar amplitude within a snowpack can be strongly influenced by spatial variability of internal layer boundaries. We quantify the impact of spatial averaging of snow stratigraphy and physical snowpack properties on surface scattering from near-nadir frequency-modulated continuous-wave radar at 12–18 GHz. Relative permittivity, density, grain size and stratigraphic boundaries were measured in-situ at high resolution along the length of a 9 m snow trench. An optimal range of horizontal averaging (4–6 m) was identified to attribute variations in surface scattering at layer boundaries to dielectric contrasts estimated from centimetre-scale measurements of snowpack stratigraphy and bulk layer properties. Single vertical profiles of snowpack properties seldom captured the complex local variability influencing near-nadir radar surface scattering. We discuss implications of scaling in-situ measurements for snow radiative transfer modelling and evaluation of airborne microwave remote sensing of snow.

KEYWORDS: radar, remote sensing, snow microstructure, snow stratigraphy, spatial variability

1. INTRODUCTION

Reliable knowledge of the mass and distribution of snow on the ground from the catchment to the global scale is essential to understand and predict cryospheric water resources, climate and natural hazards. High-resolution (~10 m) measurements of snow depth over large spatial extents (~10 km) are required to evaluate the performance of spatially distributed snow models (e.g. Marks and others, 1999; Lehning and others, 2006; Liston and Elder, 2006), as well as remote sensing observations from airborne (Liston and Sturm, 1998; Yueh and others, 2007) and satellite (Kelly, 2009; Rott and others, 2010) platforms. In seasonal snowpacks, variability in bulk properties such as depth and snow water equivalent (SWE) typically occurs over length scales of 10–100 m (e.g. Shook and Gray, 1996; Deems and others, 2006; Trujillo and others, 2007). Snow stratigraphic variability is likely to exceed that of bulk snow properties and have a shorter correlation length (<10 m) (Sturm and Benson, 2004). Variability at small scales can have a large impact on microwave measurements, particularly where contrasts in dielectric properties are strong (Marshall and others, 2005; Durand and others, 2008, 2011). Stratigraphic variability at the <10 m scale is infrequently documented (Benson and Sturm, 1993; Sturm and Benson, 2004; Domine and others, 2012; Rutter and others, 2014; King and others, 2015) due to the time consuming nature of manual stratigraphic observations. These small-scale variations may introduce large uncertainties when one-dimensional (1-D) in-situ measurements are used for comparison with distributed snow modelling and remotely sensed measurements.

Broadband frequency-modulated continuous-wave (FMCW) radar measurements at near-nadir (~0 degrees) incidence angles allow the positions of the snow surface, snow/ground interface, and internal layer boundaries to be

estimated from the propagation time of the radar returns, using an estimate of wave speed (Ellerbruch and Boyne, 1980; Gubler and Hiller, 1984; Marshall and Koh, 2008). The difference in measured time between the recorded reflection from the snow surface and the snow/ground interface, which is the travel-time of the signal in the snowpack, can be used to estimate total snow depth. The accuracy of depth estimates in dry snow is of the order of 10% using a typical velocity, and the accuracy increases with availability of in-situ density estimates (Marshall and Koh, 2008). Similarly, the thickness of stratigraphic layers can be estimated from measurements of two-way travel time between continuous reflections, when referenced to layer locations in a calibration snowpit.

As the usage of ground-based active and passive microwave measurements of snow increases (Marshall and others, 2008; Derksen and others, 2012), so too does the need to evaluate and understand snowpack layering and properties influencing radar amplitude and emission. Evaluation of microwave interactions with snowpack properties has commonly been only in one dimension, using vertical profiles of snow properties from either single or multiple snowpits within or adjacent to a sensor footprint. This employs the assumption that these properties are constant throughout the footprint (Durand and others, 2008; King and others, 2013). However, the importance of spatially distributed measurements of snowpack properties for interpretation of microwave scattering within sensor footprints has recently been demonstrated using ground-based microwave radiometers (Rutter and others, 2014) and narrowband Ku band radar (King and others, 2015). As the increased portability of broadband FMCW radar systems (Marshall and Koh, 2008; Marshall and others, 2008) enhances the potential for measurement of snowpack properties over very long

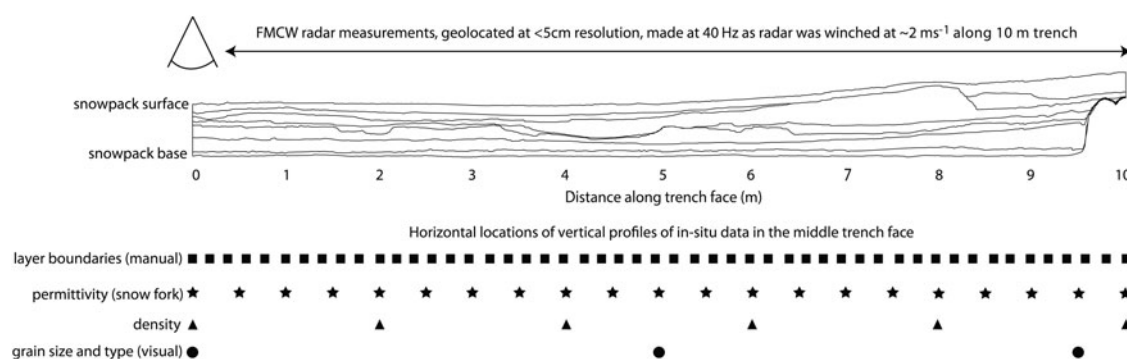


Fig. 1. Schematic diagram to illustrate the location of in-situ measurements in the middle trench face.

spatial scales, increased skill in interpreting the radar response to the snowpack is required. In particular, improved understanding of how the 2-D radar amplitude response is averaged across different spatial scales, is necessary to improve interpretation of snowpack properties over extended transects.

We collected high-resolution in-situ measurements of Arctic snowpack properties in parallel 10 m trenches, coincident with measurements of 12–18 GHz FMCW radar (see Fig. 11 in Marshall and Koh, 2008). We quantify spatial variability in snowpack stratigraphic layering at the sub-centimetre scale using Near-Infrared (NIR) photography (Matzl and Schneebeli, 2006; Tape and others, 2010), and traditional in-situ measurements of snowpack properties. Results are used to quantify the impact of spatial averaging of in-situ measurements of snowpack properties on the relationship between estimated reflectivity and radar surface scattering. Analyses focus on: (1) optimal horizontal ranges over which to spatially average in-situ measurements for comparison with nadir radar observations, and (2) horizontal averaging of radar observations using only single vertical profiles of snowpack properties (e.g. from traditional snow-pits) to adequately evaluate radar amplitude. Implications of averaging snowpack properties are discussed with relevance to evaluation of airborne microwave remote sensing of snow and simulation of electromagnetic scattering in snowpacks.

2. METHODS

2.1. Field measurements

On 23 February 2008 measurements of snowpack physical and dielectric properties were made near Toolik Lake (68° 38'N, 149°36'W), located on the North Slope of Alaska, USA. A 10 m transect was marked-out perpendicular to the edge of the north side of the lake and extended out from the shore onto lake ice. The site captured a range of snow conditions over a short horizontal extent.

FMCW radar (12–18 GHz) measurements were made ~1 m above the snow surface from antennas attached to an enclosed sled that housed radar hardware, using standard gain (20 dB) horn antennas with a 19° 3 dB beamwidth. The antennas have a maximum aperture dimension of 9 cm, giving a far-field distance at 12 and 18 GHz of 65 and 97 cm, respectively. An antenna height of ~1 m above the snow surface was chosen to place the snowpack in the far-field, to avoid complications associated with interpreting near-field measurements. The sled was very slowly winched

($<2 \text{ cm s}^{-1}$) along the transect, while recording radar measurements 40 times a second. Differential GPS (Trimble 5700) was used to geolocate the radar with an absolute horizontal accuracy of $<5 \text{ cm}$. The standard gain horn antennas have a -3 dB beamwidth of 23.75° at 12 GHz and 16.0° at 18 GHz (i.e. the angle at which the power drops by 50%). A conservative estimate of the footprint size at the base of the snowpack, based on a 1 m antenna height and 80 cm snow depth, is $75 \text{ cm} \times 75 \text{ cm}$ for 12 GHz, and $50 \text{ cm} \times 50 \text{ cm}$ at 18 GHz. The actual footprint will be somewhat smaller due to refraction at the air/snow interface. The horizontal displacement necessary to get a nearly independent sample is therefore conservatively estimated to be 1 m.

After radar measurements were made, a 10 m trench, progressively cut back in 25 cm steps to create three parallel trench faces, was excavated to span the radar footprint ($\sim 50 \text{ cm} \times 50 \text{ cm}$ at ground). The middle trench of the three excavated was located directly under the centre line of the radar profile. All trenches were cut with snow saws to be as near vertical as possible. Any artefacts resulting from the excavation process, for example teeth marks from the snow saws, were carefully removed using soft brushes and rounded wood blocks. Vertical profiles of layer boundary locations were manually measured at 20 cm intervals along each trench face. Relative hardness was the primary measurement, along with grain size and shape, used to manually distinguish layer boundaries. The horizontal positioning along the trench face of profiles of layer boundary measurements can be seen in Figure 1, in addition to the positions of all other in-situ measurements.

Prior to the hardness measurements, a series of NIR photographs (850 nm) was taken along the length of the middle trench at 35 cm intervals following the methods of Tape and others (2010). This resulted in complete coverage of the trench with $\sim 30\%$ overlap between adjacent photographs. After the NIR photography, measurements of relative permittivity were made using a Toikka (Finnish) snow fork (Sihvola and Tiuri, 1986) at 50 cm horizontal and 5 cm vertical spacing within each trench. The snow fork was inserted horizontally into the snowpack (integrating measurements over a volume of snow $\sim \pm 2 \text{ cm}$ above and below the fork), with adjacent measurements shifted slightly to alternating sides of a vertical profile to avoid any influence of disturbed snow (e.g. Marshall and others, 2005).

Destructive manual measurements of density, hardness, grain size and grain type were made after the completion of the NIR photography using standard techniques (e.g. Greene and others, 2010). Density observations were made using a 100 cm^3 box-type cutter (3 cm vertical height) at a

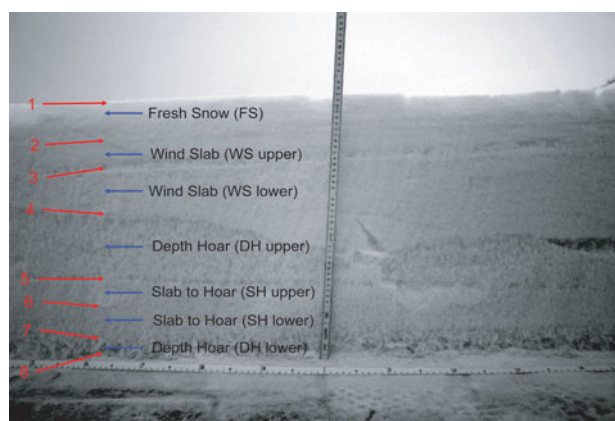


Fig. 2. NIR image of example trench section (3.5–4.5 m), annotated with layer boundaries and snow types (Table 3). Scale of horizontal measuring tape is in decimetres and vertical ruler is in centimetres.

horizontal spacing of 200 cm within individual layers. Where possible, two density samples were taken in each layer at each of the six vertical profiles along the trench. However, due to limitations of layer thicknesses and the occasional inability to get a reliable sample from each position along the trench, between 4 and 12 density samples were taken in each layer. Vertical profiles of hand hardness were used to identify layer boundaries every 20 cm along the trench, and detailed vertical profiles of grain size and grain type were made within each layer at three positions (0, 5 and 9.5 m) along the middle trench. Grain size was assessed by distributing a sample of snow grains from each layer across the field of view of a pocket microscope with a graduated reticule (0.1 mm graduations). The longest and shortest axis of a grain identified as being representative of the distribution of grains across the field of view were recorded for each layer, and detailed descriptions of the grain shapes and types were recorded. Hand hardness, grain shape and

grain type were identified using standard international conventions (Fierz and others, 2009) with the addition of a *slab-to-hoar* classification, which has previously been reported in snow cover on Alaskan lakes (Sturm and Liston, 2003). A large rock on the edge of the lakeshore caused a rapid decrease in thickness of lower layers from 9 to 10 m. This was considered an untypical influence on snow stratigraphy relative to variability in the rest of the trench. So, while measurements throughout the whole trench length are presented in Figures 2–4, analyses were limited to measurements made between 0 and 9 m (Figs 5, 6; Tables 1–3).

2.2. Data processing

Techniques used to record sub-centimetre variability in snowpack layer boundaries using NIR photography were documented in Tape and others (2010). The vertical positions of layer boundaries in this study were georeferenced relative to a ruler visible in each picture (Fig. 2). The vertical reference point for georegistration (where the base of the vertical ruler rests on the ice surface) varied between adjacent images due to localised basal roughness. Consequently, when layer boundary positions identified in adjacent images were stitched, abrupt visual discontinuities occurred, which ranged between a maximum of 2.0 and 5.4 cm for individual layer boundaries. These discontinuities were smoothed by removing boundary positions on either side of the discontinuity and then gap-filling the missing values using a cubic spline interpolation. Over all layers, 11% of the layer boundary positions were removed (ranging between 4 and 24% for each layer boundary), before being gap-filled. This minimised the influence of errors resulting from the NIR measurement process and maximised the potential for accurate representation of the true layer boundary positions. As a result, eight layer boundaries at sub-centimetre vertical resolution were identified across the length of the trench. Some

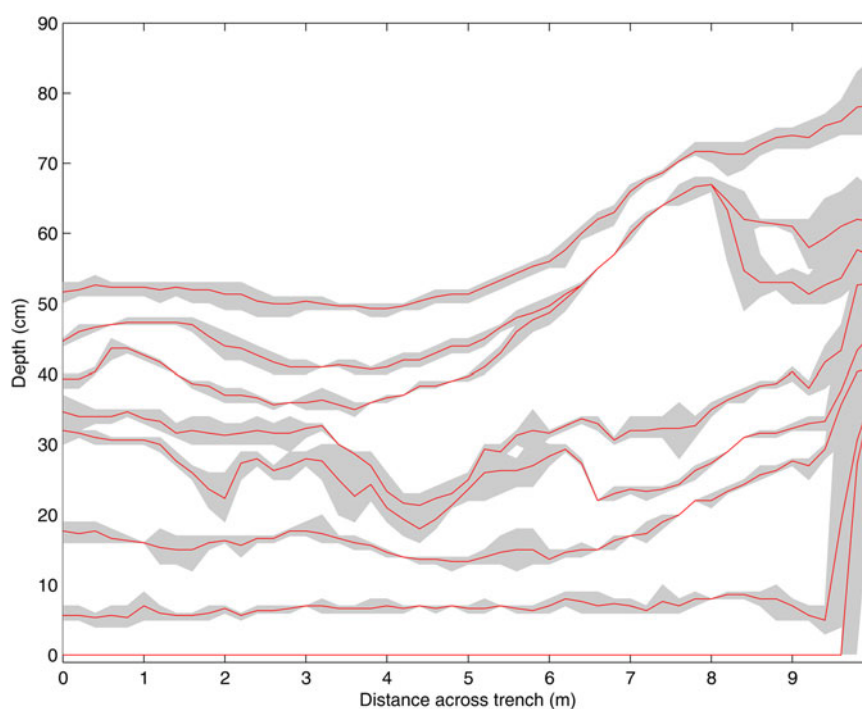


Fig. 3. Mean (red line) and range (grey area) of layer boundary positions from manual measurements at 20 cm horizontal resolution across all three trenches.

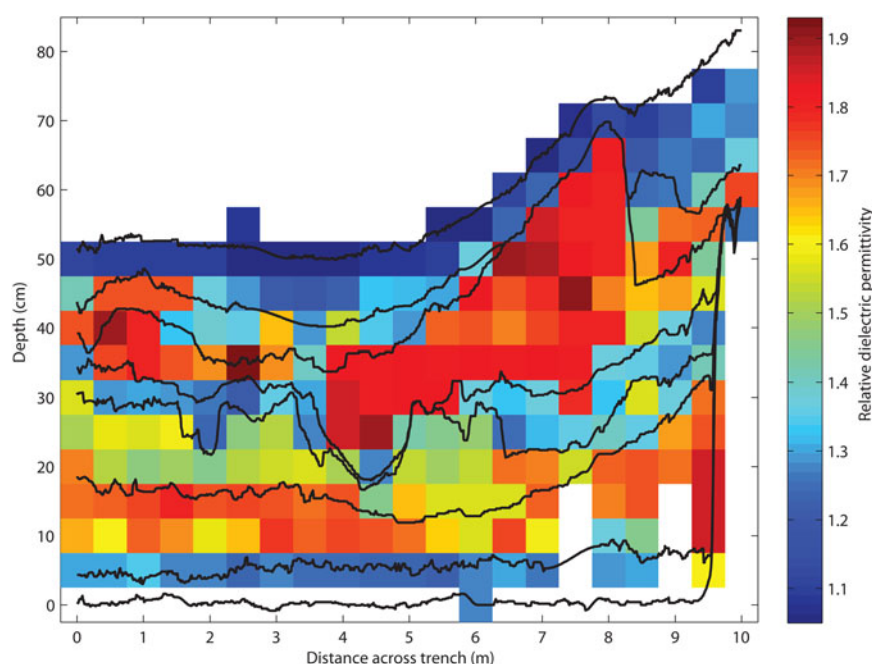


Fig. 4. Relative permittivity (Finnish snow fork) and layer boundaries (NIR photography).

differences occurred in layer boundary identification of the same trench presented by Tape and others (2010). Differences between 8 and 9 m along the trench in certain layer boundaries resulted from beneficial, a priori knowledge of manual field identification; knowledge that was intentionally made unavailable in Tape and others (2010) to allow objective evaluation of the NIR stratigraphy method.

FMCW radar observations from 12 to 18 GHz were used to maximise resolution and cover the frequency (13.95 GHz) of a coincident airborne radar experiment (Rott and others, 2009; Xu and others, 2012). Vertical resolution for nadir radar observations is inversely proportional to bandwidth; while the ultra-broad bandwidth gave a vertical resolution of 2 cm (e.g. Marshall and Koh, 2008), uncertainties in radar wave speed caused the total absolute uncertainty in location of radar amplitude to be <5 cm (e.g. Marshall and others, 2005). The profile of radar measurements was made with 98% overlapping footprints, such that the measurement spacing was 1 cm while the footprint of the measurement was ~50 cm × 50 cm. The measured radar response was corrected for spherical geometrical spreading, using a depth scale based on the mean snowpack density. These corrected data were then smoothed along the 10 m trench with a moving window median filter of 5 cm (vertical) × 50 cm (horizontal), chosen based on the vertical uncertainty and ground projected footprint.

Reflectivity was estimated using vertical gradients in electrical properties, calculated between adjacent 5 cm measurements, in the 20 vertical profiles (50 cm horizontal spacing) of in-situ relative permittivity measurements:

$$R = \left(\frac{\sqrt{\epsilon_1} - \sqrt{\epsilon_2}}{\sqrt{\epsilon_1} + \sqrt{\epsilon_2}} \right)^2 \quad (1)$$

where R is the reflectivity, and ϵ_1 and ϵ_2 are the real components of permittivity of two layers either side of a layer boundary (e.g. Ulaby and others, 1981). To compare with reflectivity, radar amplitude was averaged over a window ± 5.1 cm (vertical) and ± 1 cm (horizontal) centred around

layer boundaries. This ensured that the radar response overlapped with the positions of two adjacent relative permittivity measurements above and below layer boundaries, to be representative of the dielectric contrast across the layer boundary. Reflectivity and radar amplitude at locations other than layer boundaries were not analysed in this study.

3. RESULTS

Manual measurements showed eight major layer boundaries, including the snow surface and the snow-ice boundaries, in all three trenches across the radar footprint (Fig. 3). The mean vertical range in locations of individual layer boundaries across the three parallel trenches (Table 1), calculated from similar along-track positions in each trench, were always within 1 cm of the mean range of layer boundary positions along the length of the middle trench. Apart from the air to snow boundary, the difference between means across trenches and along the middle trench was 0.6 cm or less, and the difference between the standard deviations was 0.4 cm or less for all layer boundaries. The middle trench captured all major along-track changes in layer boundaries and as such was the sole trench used to compare with the radar measurements.

High-resolution identification of layer boundaries from NIR images captured 2-D variability in layering along the middle trench (the centre line of the radar profile). Compared with lower resolution manual measurements (20 cm horizontal, 1 cm vertical), the maximum range in layer boundary locations identified using NIR, across 40 cm moving windows of the middle trench, was higher for all boundaries (0.2–4.6 cm) other than the *Slab-to-Hoar (SH) upper to SH lower* boundary (Table 1). Consequently, while the higher resolution NIR measurements generally identify a greater range of layer boundary variability, the improvement over manual layer detection is sensitive to centimetre-scale variability in layer boundary height around the broader trend in slope.

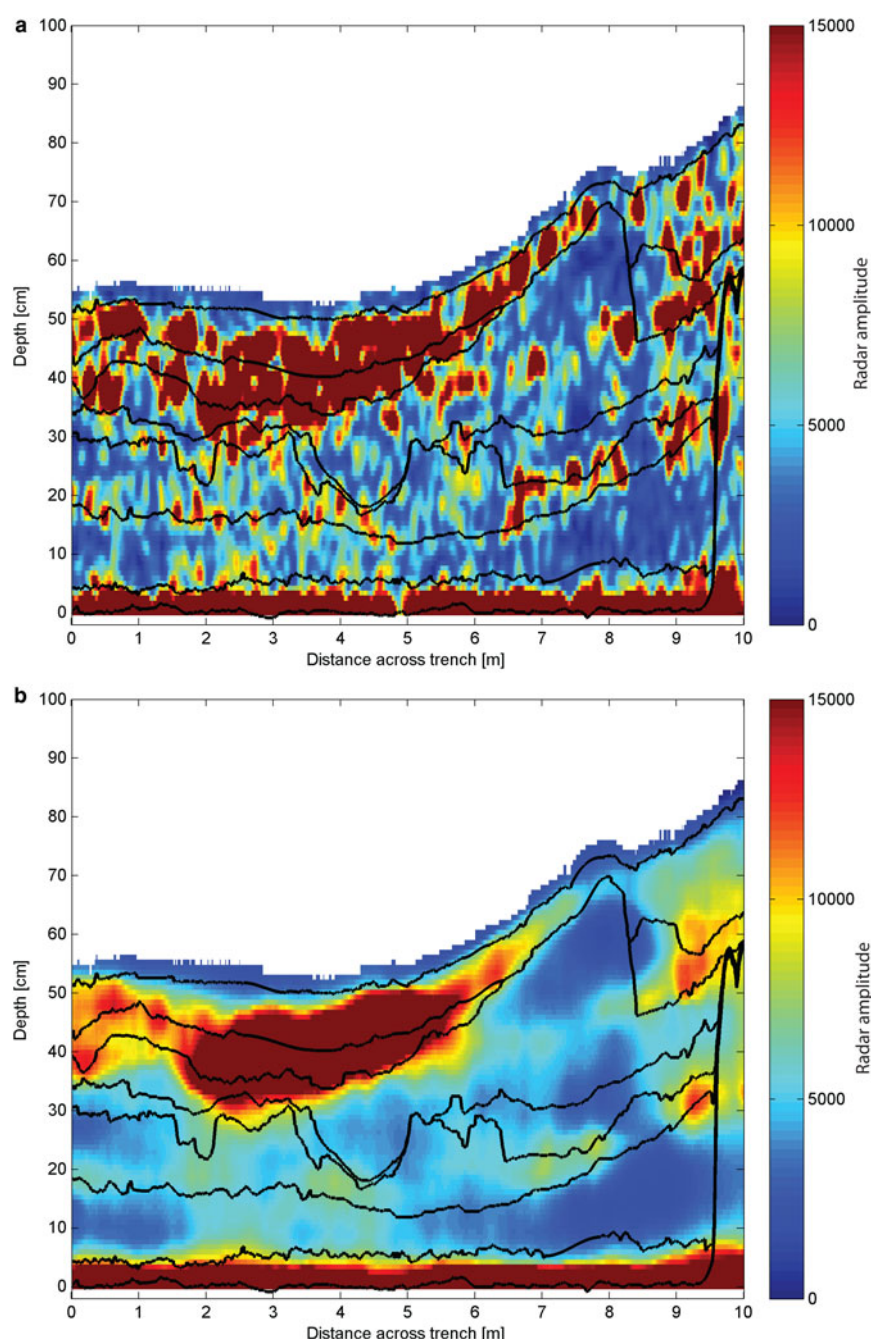


Fig. 5. (a) Corrected radar amplitude and (b) statistically smoothed radar amplitude (median over a 5 cm vertical \times 50 cm horizontal moving window) with layer boundaries (black lines) superimposed.

Layer thickness, using high-resolution NIR measurements at 1 cm horizontal resolution, indicated that means and standard deviations were similar to manual measurements made at a lower horizontal resolution (Table 2). Layer thickness measurements using NIR showed that the proportional area of individual layers within the total trench area ranged between 8 and 24% (Table 2). Thicknesses of individual layers varied greatly along the trench with standard deviations from 1.4 to 9.4 cm. Also, of the seven major layers present (Fig. 2) two, *Wind Slab (WS) upper* and *Depth Hoar (DH) upper*, were discontinuous (Fig. 3). Layer thickness variability is shown in Table 2, where the range in the maximum percentage that an individual layer occupied within any single vertical profile varied between 49% (*WS lower*) and 13% (*DH lower*) along the trench.

Density measurements indicated that between-layer variability was much greater than the inter-layer variability (Table 3); mean density of each layer ± 1 standard deviation did not overlap the mean density of adjacent layers. The range of grain size short axis was small (0.2–1.7 mm) across all layers, but the range in the long axis was much larger (0.8–5.3 mm). Consequently, long axis grain size helped highlight differences between layers, especially transitions between wind slab, depth hoar and slab-to-hoar. Increases or decreases in hardness from layer to layer were generally in-phase with density. However, hardness also allowed more subtle differences between layers to be identified, such as between the upper and lower wind slab layers, where the hardness strongly transitioned between 1-finger and knife despite density and grain size not changing greatly.

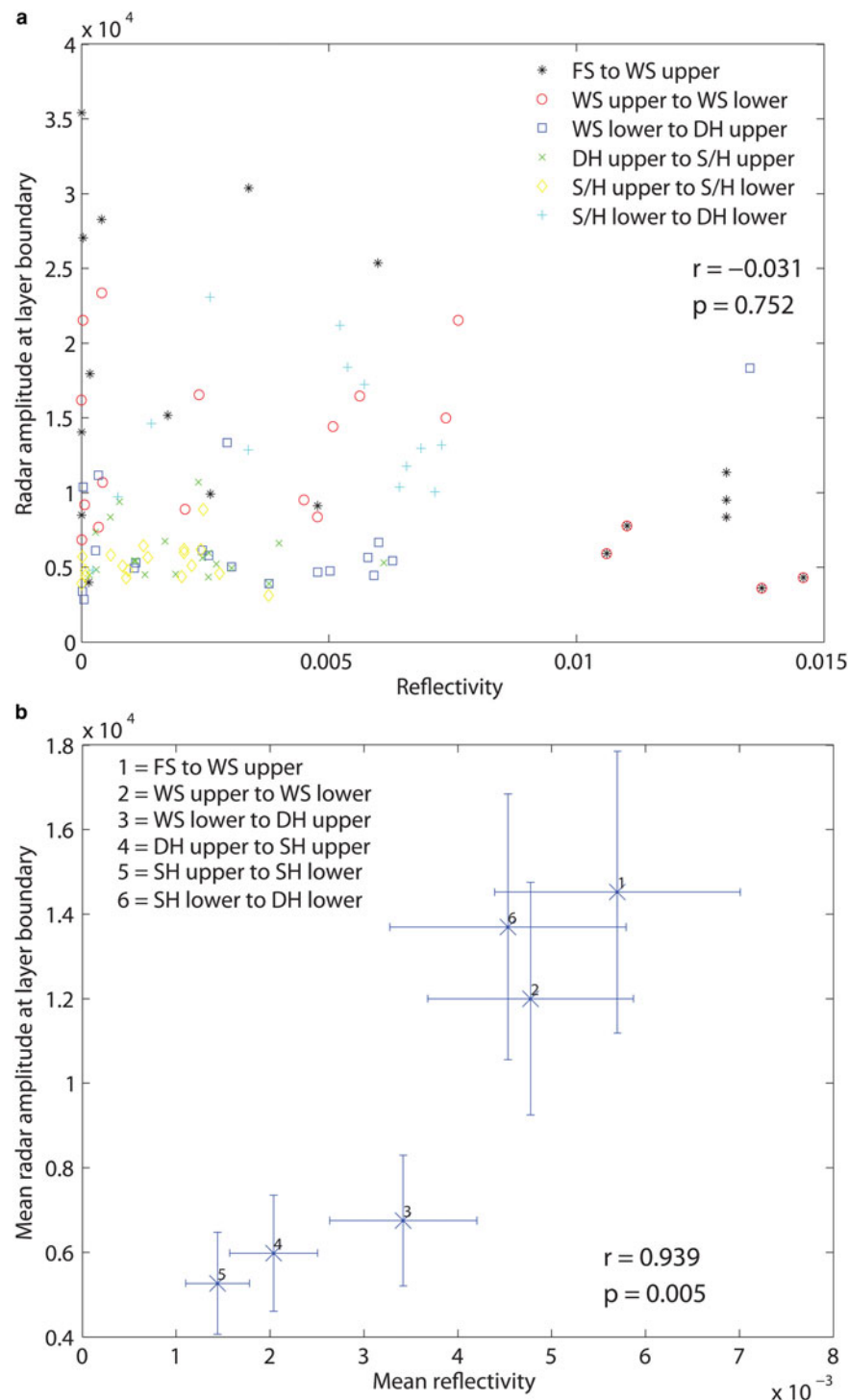


Fig. 6. Scatterplots of (a) paired reflectivities and radar amplitude across layer boundaries, and (b) mean reflectivities and smoothed radar amplitude across layer boundaries excluding surface and basal boundaries (error bars are one standard error of the mean).

Layer boundaries were overlaid on regularly-spaced, 2-D grids of the real component of measured relative permittivity (Fig. 4) and radar amplitude (Fig. 5a). Major layer boundaries spatially delineate layers with relatively low permittivity (e.g. *FS*, *DH upper* and *DH lower*) and relatively high permittivity (e.g. *WS lower*, *SH lower*). Radar amplitude, though highly spatially variable, showed some consistent structure along the trench. The smoothed amplitude (median values of 5 cm vertical by 50 cm horizontal moving windows) better resembled the volume of the snowpack represented by the radar signal and the relative consistency of surface scattering at layer boundaries (Fig. 5b). Strong radar amplitude was

evident continuously along the *DH lower* to *Ice* boundary, and discontinuously along the *FS* to *WS upper* and *WS upper* to *WS lower* boundaries. There was a large decrease in radar amplitude in the *FS* to *WS* boundaries between 7.5 and 8.5 m along the trench. Areas of moderate amplitude were evident around the *DH upper* to *SH upper*, and *SH upper* to *SH lower* layer boundaries, but were less consistent along the trench than areas of high-radar amplitude.

Although there was poor correlation between all individual pairs of radar amplitude and in-situ estimated reflectivity across layer boundaries (Fig. 6a: $r = -0.03$, $p = 0.752$), there was a very significant positive correlation (Fig. 6b: $r = 0.94$,

Table 1. Range statistics (in cm) of boundary layer positions between 0 and 9 m of the three trenches within the radar profile

Measurement type	Number of trenches	Calculation of range	Statistic	Air to FS	FS to WS upper	WS upper to WS lower	WS lower to DH upper	DH upper to SH upper	SH upper to SH lower	SH lower to DH lower	DH lower to Ice
Manual measurement	All three trenches	Single horizontal positions	Mean	2.4	1.9	2.3	2.6	3.0	1.9	1.7	0.0
			SD	0.9	1.4	2.9	1.5	2.5	1.5	1.1	0.0
	Middle trench	40 cm horizontal moving window	Mean	1.4	2.1	3.1	2.4	3.2	1.6	1.1	0.0
			SD	1.3	1.8	3.1	1.7	2.2	1.1	0.8	0.0
NIR measurement	Middle trench	40 cm horizontal moving window	Max	4	8	19	8	9	5	3	0
			Max	5.2	11.1	23.6	9.5	10.7	3.6	3.2	1.7

Table 2. Layer thickness statistics in the middle trench between 0 and 9 m using manual and NIR measurements

Layer	Manual		NIR			
	Layer thickness cm		Layer thickness cm		% of total trench area	% of any single vertical profile across trench
	Mean	SD	Mean	SD		
FS	7.2	2.3	8.0	1.8	14	5
WS upper	5.6	2.0	6.0	3.2	8	0
WS lower	14.2	9.1	13.9	9.4	24	2
DH upper	5.5	2.6	4.8	2.7	8	0
SH upper	9.2	3.9	9.4	3.7	16	4
SH lower	10.4	3.4	11.0	3.0	19	11
DH lower	6.8	1.2	5.4	1.4	9	4

Table 3. Snow layer properties between 0 and 9 m

Layer	Density			Mean grain size		Hardness	Snow type
	Mean kg m ⁻³	SD kg m ⁻³	Sample size	Shortest axis mm	Longest axis mm		
FS	75	16	12	0.5	1.5	4 fingers	Recent, fragmented precipitation particles
WS upper	356	51	10	0.2	0.8	1 finger	Wind slab, sintered particles
WS lower	411	36	12	0.3	1	Knife	Wind slab, sintered particles
DH upper	238	21	4	1.7	5.3	1 finger	Depth-hoar columns
SH upper	324	33	12	0.8	2.7	pencil	Slab-to-hoar, depth-hoar columns
SH lower	375	37	12	0.6	2	pencil	Slab-to-hoar, depth-hoar columns
DH lower	248	49	6	1.5	7	1 finger	Depth-hoar columns

$p < 0.05$) between the mean reflectivities and mean smoothed radar amplitude for each of the six internal boundaries, averaged along the trench. Of the three layer boundaries with the largest reflectivities, the high-radar amplitude attributed to the *SH lower* to *DH lower* boundary was partly influenced by very strong amplitude within the averaging window from the adjacent *DH lower* to *Ice* boundary. While surface scattering from layer boundaries increased with increased reflectivity as expected, the variability (expressed as error bars of one standard error of the mean in Fig. 6b) also increased with increased mean values. The effect of multi-path signals will not impact on this variability as reflectivity values at layer interfaces are < 0.015 in all cases, with mean values < 0.006 (see Fig. 6), meaning any multipath signal will be at least 2500 times smaller than a

direct reflection from a layer boundary. In addition, the reduction in radar energy reaching the lower layer boundaries as a consequence of being reflected at upper boundaries is very small. As reflectivity values are less than 0.015, the total incoming radar energy at the lower boundaries is only a few percent lower than the total incoming radar energy at the upper boundaries.

When the horizontal averaging distance was adjusted from 0 to 9 m in increments of 0.5 m (Fig. 7), where correlation sample size (n) decreased from 107 to 4, correlations became statistically significant ($p < 0.05$) at horizontal averaging distances of 4 m ($n = 52$). Correlation coefficients continued to increase rapidly up to an averaging distance of 6 m ($n = 30$), after which the rate of increase in correlation reduced substantially. If the layer averages of radar amplitude

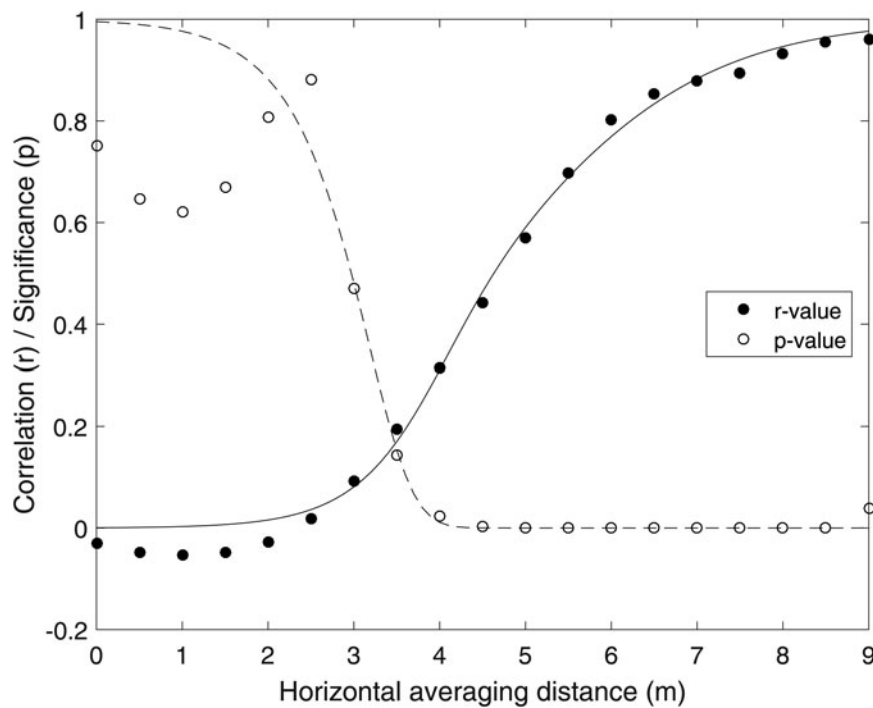


Fig. 7. Correlation coefficients and statistical significance between radar amplitude and reflectivity when averaged over increasing horizontal extents. Solid line is given by Eqn (7) with parameters fitted to the data by nonlinear least squares, dashed line is p calculated for r from Eqn (7) and sample size (n) from data.

and reflectivity are A_0 and R_0 with between-layer standard deviations σ_A and σ_R , the correlation between layer averages is

$$\rho = \frac{\text{cov}(A_0, R_0)}{\sigma_A \sigma_R}. \quad (2)$$

Suppose that the measurements of radar amplitude and reflectivity can be expressed as sums

$$A = A_0 + \varepsilon_A \quad (3)$$

and

$$R = R_0 + \varepsilon_R \quad (4)$$

where ε_A and ε_R represent spatial variability and measurement errors with standard deviations $\sigma_{\varepsilon A}$ and $\sigma_{\varepsilon R}$, giving signal to noise ratios $SNR_A = \sigma_A^2 / \sigma_{\varepsilon A}^2$ and $SNR_R = \sigma_R^2 / \sigma_{\varepsilon R}^2$. Assuming exponential spatial autocorrelations with correlation lengths L_A and L_R , the variances of measurements averaged over a distance L are

$$s_A^2 = \sigma_A^2 + \sigma_{\varepsilon A}^2 e^{-L/L_A} = (1 + SNR_A^{-1} e^{-L/L_A}) \sigma_A^2 \quad (5)$$

and

$$s_R^2 = \sigma_R^2 + \sigma_{\varepsilon R}^2 e^{-L/L_R} = (1 + SNR_R^{-1} e^{-L/L_R}) \sigma_R^2. \quad (6)$$

Reducing error by averaging measurements with autocorrelated noise requires repeated measurements spread over distances that are large compared with the correlation length. If there is no correlation between ε_B and ε_R , the correlation between horizontally-averaged measurements is

$$r = \frac{\text{cov}(A, R)}{s_A s_R} = \frac{\rho}{(1 + SNR_A^{-1} e^{-L/L_A})^{-1/2} (1 + SNR_R^{-1} e^{-L/L_R})^{-1/2}} \quad (7)$$

i.e. noise reduces the measured correlation towards 0 but horizontal averaging increases it towards ρ . The parameters in Eqn (7) were fitted to data in Figure 7 by nonlinear least squares, giving SNR of 4×10^{-5} and 7.5×10^{-3} and correlation lengths of 0.4 and 1.1 m; the correlation function is symmetric between reflectivity and radar amplitude so does not distinguish which is which. The low SNR are necessary to match the very low correlations for short averaging lengths. Equation (7) cannot reproduce the small and statistically insignificant negative correlation found for measurements averaged over distances of $< \sim 2$ m, but the fitted curves otherwise follow the observations closely.

The impact of spatial averaging on correlation across a trench is important for accurate assessment of spatial variability in snowpack reflectivity. However, it is also of great practical interest to quantify the improved correlation resulting from identifying layer boundaries in two dimensions using NIR photography, rather than horizontally extrapolating layer boundaries from a single vertical profile in a snowpit. To investigate, the vertical positions of layer boundaries were extrapolated horizontally between 0 and 9 m from each of the individual 19 available vertical profiles across the trench and correlations between radar amplitude and in-situ reflectivity were calculated. Only one vertical profile (at 6.5 m along the trench) provided a significant correlation ($r = 0.83$, $p < 0.05$). When all 19 single vertical profiles were considered collectively, correlations between radar amplitude and reflectivity were low (r -values: mean = 0.16, standard deviation = 0.32).

4. DISCUSSION AND CONCLUSIONS

Variations in layer thickness were evident throughout the 9 m trench. Increased snow depth from left to right across the trench did not result in a proportional thickening of all

internal layers. Instead, the upper wind slab layer and the lower slab-to-hoar layer increased in thickness at the expense of all other layers, most likely due to wind redistribution. Reduction in layer thickness often occurred where layers were structurally weak, for example in the upper depth hoar layer, which may have been scoured by wind. Observed layer expansion and contraction confirmed that even in the absence of melt, rough subnivean topography, or underlying vegetation, complex stratigraphic layering can develop in a similar manner to snow on tundra (e.g. Sturm and Benson, 2004; Domine and others, 2012). Such high horizontal variability in snowpack layer thickness and the vertical position of layer boundaries has important implications for: (1) spatial averaging of field measurements of physical snowpack properties used to interpret co-located variability in radar amplitude, and (2) one- and two-dimensional simulation of electromagnetic scattering in snow.

Mean values of near-nadir radar amplitude and in-situ reflectivity at layer boundaries, located at a centimetre-scale, were correlated ($p < 0.05$) when considered across a 9 m horizontal extent of an Arctic snowpack. Where high-resolution layer boundary measurements were available, there was an optimum range of horizontal averaging between 4 and 6 m to capture interactions among radar amplitude, stratigraphy and bulk layer properties. Averaging below 4 m, the correlation was statistically insignificant and above 6 m the rate of increase in the correlation markedly decreased. In addition, horizontal extrapolation across the trench of layer boundaries taken from single vertical profiles, which are representative of more commonly available snow pit measurements, very rarely demonstrated a significant correlation between radar amplitude and reflectivity. This suggests that conventional field measurement techniques involving vertical profiles of snowpack stratigraphy may not capture the spatial variability required for evaluation of near-nadir radar observations. Instead, it strengthens the argument (cf. Derksen and others, 2009) for the use of field techniques, such as NIR photography, to capture sub-centimetre scale variability in snowpack stratigraphy.

While ground-based FMCW radar offers the potential for orders of magnitude more measurements than snowpit or trench measurements, improved interpretation of radar amplitude will be necessary to enhance evaluation within sensor footprints for calibration and validation campaigns of future satellite sensors (e.g. Cline and others, 2003; Yueh and others, 2009; Rott and others, 2010). In addition, although most radar measurements on airborne and satellite platforms are made at off-nadir incidence angles (30° – 45°), internal layer boundaries, if they are not horizontal and are rough at the wavelength scale, add uncertainty to estimates of volume scattering, which increases in dominance relative to scattering at internal layer interfaces as incidence angles move away from nadir. Improved knowledge of changes in snowpack properties from nadir FMCW amplitude observations may, therefore, provide important information when interpreting off-nadir radar amplitude. The increase in variability with increasing mean radar amplitude and in-situ reflectivity, indicated by increasing error bars in Figure 6b, suggests a need to measure layer boundaries at the centimetre scale across a sufficiently characteristic range of variability that might be expected within sensor footprints. While the horizontal resolution of a remotely sensed measurement depends on the sensor antenna pattern and the altitude above the earth's surface, previous experiments have

averaged airborne off-nadir Ku band radar measurements to 200 m grids (Yueh and others, 2009). These grids were evaluated using in-situ measurements consisting of five snowpit profiles of snowpack properties and hundreds of snow depths, at 10–20 m spacing in an 'hourglass' pattern, within 500×500 m areas of Colorado, USA. While this is relatively data-rich for in-situ evaluation of airborne measurements, it gives an indication of data paucity for considering the impact of local stratigraphic variability on radar amplitude.

The high horizontal variability of layer thickness in proportion to total depth also has important implications for computational electromagnetic models that describe scattering of microwave energy in snow (Tsang and others, 2013). In particular, it suggests that 1-D simulations for calibration or validation studies should use an ensemble approach to account for multiple stratigraphic possibilities, resulting in a distribution of simulated radar amplitude values to compare with measurements. Also, some electromagnetic models, which simulate scattering and absorption of microwave energy within layers as well as scattering at major dielectric boundaries can be used in a 2-D manner (e.g. Tsang and others, 2007), requiring realistic 2-D initialisation. Consequently, datasets containing measurements of radar response and snowpack properties at the spatial resolutions presented here are strongly suggested for future sensitivity experiments evaluating simulated narrowband, off-nadir radar amplitude.

This study has presented a detailed set of ground-based measurements to examine the impact of spatial averaging of in-situ snow stratigraphy and physical snowpack properties on variability in FMCW radar (12–18 GHz) amplitude. In doing so, an optimum range of horizontal averaging (4–6 m) was identified to capture centimetre-scale interactions between radar amplitude, snowpack stratigraphy and the bulk layer properties, which controlled reflectivity within an Arctic snowpack. Single vertical profiles of snowpack properties were highly unlikely to represent the local spatial variability in snowpack properties that influenced near-nadir radar amplitude. Future study will be required to assess how these implications for interpretation of amplitude from portable FMCW radar, would up-scale to airborne and satellite footprints, as well as entire hydrological catchments.

ACKNOWLEDGEMENTS

We thank M. Sturm, J. Holmgren, K. Elder, D. Cline and the winter crew at the University of Alaska Fairbanks Toolik Lake research facility for technical and logistical support. We thank the editor and two anonymous reviewers for their detailed and helpful comments on a previous version of the manuscript. Financial support through UK Natural Environment Research Council (NERC) Fellowship NE/E013902/1 (Rutter) and NASA THP/NEWS NNG06GE70G (Marshall) is gratefully acknowledged.

REFERENCES

- Benson CS and Sturm M (1993) Structure and wind transport of seasonal snow on the Arctic slope of Alaska. *Ann. Glaciol.*, **18**, 261–267
- Cline DW and 10 others (2003) An overview of the NASA Cold Land Processes Field Experiment (CLPX-2002). In Kummerow CD, Jiang J and Uratuka S, eds. *Microwave Remote Sensing of the Atmosphere and Environment III*. Hangzhou, China, 361–372

- Deems JS, Fassnacht SR and Elder KJ (2006) Fractal distribution of snow depth from lidar data. *J. Hydrometeorol.*, **7**(2), 285–297 (doi: 10.1175/JHM487.1)
- Derksen C and 6 others (2009) Northwest territories and nunavut snow characteristics from a subarctic traverse: implications for passive microwave remote sensing. *J. Hydrometeorol.*, **10**(2), 448–463 (doi: 10.1175/2008jhm1074.1)
- Derksen C and 6 others (2012) Evaluation of passive microwave brightness temperature simulations and snow water equivalent retrievals through a winter season. *Remote Sens. Environ.*, **117**, 236–248 (doi: 10.1016/j.rse.2011.09.021)
- Domine F, Gallet J-C, Bock J and Morin S (2012) Structure, specific surface area and thermal conductivity of the snowpack around Barrow, Alaska. *J. Geophys. Res.*, **117**, D00R14 (doi: 10.1029/2011JD016647)
- Durand M, Kim EJ and Margulis SA (2008) Quantifying uncertainty in modeling snow microwave radiance for a mountain snowpack at the point-scale, including stratigraphic effects. *IEEE Trans. Geosci. Remote Sens.*, **46**(6), 1753–1767 (doi: 10.1109/TGRS.2008.916221)
- Durand M, Kim EJ, Margulis SA and Molotch NP (2011) A first-order characterization of errors from neglecting stratigraphy in forward and inverse passive microwave modeling of snow. *IEEE Geosci. Remote Sens. Lett.*, **8**(4), 730–734 (doi: 10.1109/lgrs.2011.2105243)
- Ellerbruch DA and Boyne HS (1980) Snow stratigraphy and water equivalence measured with an active microwave system. *J. Glaciol.*, **26**(94), 225–233
- Fierz C and 8 others (2009) *The international classification for seasonal snow on the ground*. IHP-VII Technical Documents in Hydrology No.83, IACS Contribution No. 1, UNESCO-IHP, Paris
- Greene E and 11 others (2010) *Snow, weather and avalanches: observation guidelines for avalanche programs in the United States*. American Avalanche Association, Pagosa Springs, Colorado
- Gubler H and Hiller M (1984) The use of microwave FMCW radar in snow and avalanche research. *Cold Regions Sci. Technol.*, **9**(2), 109–119
- Kelly R (2009) The AMSR-E snow depth algorithm: description and initial results. *J. Remote Sens. Soc. Japan*, **29**, 307–317 (doi: 10.11440/rssj.29.307)
- King J and 5 others (2013) UW-Scat – a ground-based dual frequency scatterometer for observation of snow properties. *IEEE Geosci. Remote Sens. Lett.*, **10**(3), 528–532 (doi: 10.1109/LGRS.2012.2212177)
- King J and 7 others (2015) Spatio-temporal influence of tundra snow properties on Ku-band (17.2 GHz) backscatter. *J. Glaciol.*, **61** (226), 267–279 (doi: 10.3189/2015JG14J020)
- Lehning M and 5 others (2006) ALPINE3D: a detailed model of mountain surface processes and its application to snow hydrology. *Hydrol. Process.*, **20**(10), 2111–2128 (doi: 10.1002/hyp.6204)
- Liston GE and Elder K (2006) A distributed snow-evolution modeling system (SnowModel). *J. Hydrometeorol.*, **7**(6), 1259–1276 (doi: 10.1175/JHM548.1)
- Liston GE and Sturm M (1998) A snow-transport model for complex terrain. *J. Glaciol.*, **44**(148), 498–516
- Marks D, Domingo J, Susong D, Link T and Garen D (1999) A spatially distributed energy balance snowmelt model for application in mountain basins. *Hydrol. Process.*, **13**(12–13), 1935–1959 (doi: 10.1002/(SICI)1099-1085(199909)13:12/13<1935::AID-HYP868>3.0.CO;2-C)
- Marshall HP and Koh G (2008) FMCW radars for snow research. *Cold Regions Sci. Technol.*, **52**(2), 118–131 (doi: 10.1016/j.coldregions.2007.04.008)
- Marshall HP, Koh G and Forster RR (2005) Estimating alpine snowpack properties using FMCW radar. *Ann. Glaciol.*, **40**, 157–162
- Marshall HP, Koh G and Sturm M (2008) Ultra-broadband portable microwave FMCW radars for measuring snow depth, snow water equivalent, and stratigraphy: practical considerations. In *Proceedings of the XXIXth International Union of Radio Science (URSI) General Assembly*
- Matzl M and Schneebeli M (2006) Measuring specific surface area of snow by near-infrared photography. *J. Glaciol.*, **52**(179), 558–564 (doi: 10.3189/172756506781828412)
- Rott H, Heidinger M, Nagler T, Cline D and Yueh S (2009) Retrieval of snow parameters from Ku-band and X-band radar backscatter measurements. *IEEE Int. Geosci. Remote Sens. Symp.*, **1–5**, 395–398 (doi: 10.1109/IGARSS.2009.5418024)
- Rott H and 13 others (2010) Cold regions hydrology high-resolution observatory for snow and cold land processes. *Proc. IEEE*, **98**(5), 752–765 (doi: 10.1109/JPROC.2009.2038947)
- Rutter N and 7 others (2014) Snow stratigraphic heterogeneity within ground-based passive microwave radiometer footprints: implications for emission modeling. *J. Geophys. Res.: Earth Surf.*, **119** (doi: 10.1002/2013JF003017)
- Shook K and Gray DM (1996) Small-scale spatial structure of shallow snowcovers. *Hydrol. Process.*, **10**(10), 1283–1292 (doi: 10.1002/(SICI)1099-1085(199610)10:10<1283::AID-HYP460>3.0.CO;2-M)
- Sihvola A and Tiuri M (1986) Snow fork for field determination of the density and wetness profiles of a snow pack. *IEEE Trans. Geosci. Remote Sens.*, **24**(5), 717–721
- Sturm M and Benson C (2004) Scales of spatial heterogeneity for perennial and seasonal snow layers. *Ann. Glaciol.*, **38**, 253–260 (doi: 10.3189/172756404781815112)
- Sturm M and Liston GE (2003) The snow cover on lakes of the Arctic Coastal Plain of Alaska, USA. *J. Glaciol.*, **49**(166), 370–380 (doi: 10.3189/172756503781830539)
- Tape KD, Rutter N, Marshall HP, Essery R and Sturm M (2010) Recording microscale variations in snowpack layering using near-infrared photography. *J. Glaciol.*, **56**(195), 75–80 (doi: 10.3189/002214310791190938)
- Trujillo E, Ramirez JA and Elder KJ (2007) Topographic, meteorologic, and canopy controls on the scaling characteristics of the spatial distribution of snow depth fields. *Water Resour. Res.*, **43** (7), W07409 (doi: 10.1029/2006WR005317)
- Tsang L and 5 others (2007) Modeling active microwave remote sensing of snow using dense media radiative transfer (DMRT) theory with multiple-scattering effects. *IEEE Trans. Geosci. Remote Sens.*, **45**(4), 990–1004 (doi: 10.1109/TGRS.2006.888854)
- Tsang L, Ding K-H, Huang S and Xu X (2013) Electromagnetic computation in scattering of electromagnetic waves by random rough surface and dense media in microwave remote sensing of land surfaces. *Proc. IEEE*, **101**(2), 255–279 (doi: 10.1109/JPROC.2012.2214011)
- Ulaby FT, Moore RK and Fung AK (1981) *Microwave remote sensing: active and passive, volume 1: Microwave remote sensing fundamentals and radiometry*. Addison-Wesley, Advanced Book Program, Reading, MA
- Xu X, Tsang L and Yueh S (2012) Electromagnetic models of Co/Cross polarization of bicontinuous/DMRT in radar remote sensing of terrestrial snow at X- and Ku-band for CoReH2O and SCLP applications. *IEEE J. Selected Topics Appl. Earth Observ. Remote Sens.*, **5**(3), 1024–1032 (doi: 10.1109/JSTARS.2012.2190719)
- Yueh S, Cline D and Elder K (2007) Airborne Ku-band radar remote sensing of terrestrial snow cover. In *IGARSS: 2007 IEEE International Geoscience and Remote Sensing Symposium, Vols 1–12 – Sensing and Understanding Our Planet*, 1211–1214 (doi: 10.1109/IGARSS.2007.4423023)
- Yueh SH and 5 others (2009) Airborne ku-band polarimetric radar remote sensing of terrestrial snow cover. *IEEE Trans. Geosci. Remote Sens.*, **47**(10), 3347–3364 (doi: 10.1109/tgrs.2009.2022945)

MS received 9 February 2016 and accepted in revised form 21 June 2016